Workshop on Nonlinear Analysis and Control Theory in
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Constrained control in reaction-diffusion equations

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Abstract

The classical control theory for parabolic equations does not take into account the fact that specific reaction-diffusion equations make physically sense only if the state is within [0, 1], in case that the solution has to model a proportion. The talk will concern the techniques developed in [1, 2, 3, 4] in order to obtain control strategies satisfying the modelling constraints. Furthermore, it will be observed, under certain criteria, the lack of controllability due to the imposition of state constraints.

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References

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