



Workshop on Nonlinear Analysis and Control Theory in  
Honor of Professor Enrique Zuazua for his 60th birthday

November 3–5, 2021 – Virtual Format

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# Exponential convergence towards consensus for non-symmetric linear first-order systems in finite and infinite dimensions

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## Abstract

I will first recall some results on how to achieve consensus for well known classes of systems, like the celebrated Cucker-Smale or Hegselmann-Krause models. When the systems are symmetric, convergence to consensus is classically established by proving, for instance, that the usual variance is an exponentially decreasing Lyapunov function: this is a “ $L^2$  theory”. When the systems are not symmetric, no  $L^2$  theory existed until now and convergence was proved by means of a “ $L^\infty$  theory”. In this talk I will show how to develop a  $L^2$  theory by designing an adequately weighted variance, and how to obtain the sharp rate of exponential convergence to consensus for general finite and infinite-dimensional linear first-order consensus systems. If time allows, I will show applications in which one is interested in controlling vote behaviors in an opinion model.

Joint work with:

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## References

- [1] BOUDIN, LAURENT; SALVARANI, FRANCESCO; TRÉLAT, EMMANUEL, *Exponential convergence towards consensus for non-symmetric linear first-order systems in finite and infinite dimensions*, Preprint Hal (2021), 18 pages.

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